# **Astrophysics of Neutron Stars : Introduction**

# Sushan Konar



Astronomy from Archival Data

An IAU-OAD Project

2020

Sushan Konar

Astrophysics of Neutron Stars

# Archival data may be thought of as any sort of information,

previously collected by others, amenable to systematic study.

# **Introduction :**

- The Discovery
- The Extreme Physics
- The Radio Pulsar
- Timing & Null

# **The Discovery**

# The Concept : 1930s

• February 1931 : Landau completes work on maximum mass of white dwarf.

$$M_{
m max}=rac{3.1}{m^2}\left(rac{\hbar c}{G}
ight)^{rac{3}{2}}$$

Predicts existence of 'giant atomic nuclei'-like stars.

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- 17 February 1932 : Chadwick submits neutron discovery paper to Nature.
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• 15 January 1934 : The abstract of their talk is published.

[Note :  $E_{
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m SNII} \sim 10^{51}$  erg  $<< E_{
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- 1. Landau L. D., Phys. Z. Sowjetunion, 1, 285 (1932)
- 2. & 3. Baade W., Zwicky F., Proc. National Acad. Sci., 20, 254 & 259 (1934)
- 3. Baade W., Zwicky F. Phys. Rev. 46 76 (1934)

Chandrasekhar S., ApJ, 74, 81 (1931)

Yakovlev D. G., Haensel P., Baym G., Pethick C. J., Physics Uspekhi, 56 (3), 289 (2013)

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# The Discovery : 1960s

• 1965 : Antony Hewish & Samuel Okoye observe "..an unusual source of high radio brightness temperature in the Crab Nebula.".

Crab pulsar was detected in 1968.



Credit : Optical - NASA/HST/ASU/J. Hester et al., X-Ray - NASA/CXC/ASU/J. Hester et al.

- 1967 : Jocelyn Bell & Antony Hewish detect regular radio pulses from CP1919 (PSR J1921+2153).
  - *P* = 1.33 s, keeping sidereal time First detection of a radio pulsar.



Hewish A., Bell S. J., Pilkington J. D. H., Scott P. F., Collins R. A., Nature 217 709 (1968)

# The Discovery : 1960s

 1971 : Giacconi et al. discover 4.8 s X-ray pulsations in Cen X-3.

### *First detection of an X-ray pulsar. Cen X-3 is a high-mass X-ray binary.*

# X-Ray Pulsar Cen X-3



Figure 5. X-ray pulsations of Cen X-3. From Giacconi, 1974.

#### Pulses occur at intervals of 4.84 seconds

Giacconi, R. et al., ApJ, 167, L67 (1971)

- 1964 : Lodewijk Woltjer, from magnetic flux conservation, estimates  $B_{\rm NS} \sim 10^{14} 10^{16}$  G.
- 1967, 1968 : Franco Pacini indicates likelihood of strong radiation from rotating magnetised neutron stars, which may power supernova remnants (Crab Nebula).
- 1968, 1969 : Thomas Gold develops a similar model to explain radiation from CP1919.
- 1969 : Radhakrishnan & Cook; Gunn & Ostriker; Goldreich & Julian - radio pulsar model.



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# **The Extreme Physics**

## **The End States**

- Failed Stars :  $M < 80 M_{Jupiter} (M_{Jupiter} \simeq 0.001 M_{\odot})$ 
  - Giant Planets *M* < 13 *M*<sub>Jupiter</sub>, no fusion
  - Brown Dwarfs 13  $M_{Jupiter} < M < 80 M_{Jupiter}$ , D<sup>2</sup> fusion
- Stellar Remnants Compact Stars
  - White Dwarfs
  - Neutron Stars
  - Black Holes

Gravity Defied I - IV, Resonance, March - June, 2017, Sushan Konar

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#### **The Active Phase**



Fusion Chain -  $H^1 \rightarrow He^4 \rightarrow Be^8 \rightarrow C^{12}.. \rightarrow Fe^{56}$ 

*No 'exothermic' fusion beyond Fe*<sup>56</sup>. (*Fe*<sup>56</sup> - minimum binding energy/nucleon )

No radiative pressure support beyond iron peak elements.

Figure credit : Sushan Konar

# **Stellar Remnants**



# **Dimensions :**

•  $M \sim 1-3~{
m M}_{\odot}~~({
m M}_{\odot}\sim 2 imes 10^{33}~{
m gm})$ 

 $M \simeq 2.14 \ M_{\odot}$ , Cromatie H. T. et al., Nature Astronomy, 2019

• *R* ~ 10 – 15 Km

# **Compact Structure : Consequences**

• Binding Energy :  $E_B \simeq \frac{GM^2}{B} \sim 10^{53}$  erg

• GR Effects : Schwarzschild factor -  $\frac{2GM}{Bc^2} \sim 0.3$ 

# **Dimensions :**

- $M \sim 1-3~{
  m M}_{\odot}~~({
  m M}_{\odot} \sim 2 imes 10^{33}~{
  m gm})$
- $R \sim 10-15~{
  m Km}$

# **Compact Structure : Consequences**

• Fast Rotation : 
$$P_{\text{spin}}^{\min} = 2\pi \left(\frac{r^3}{GM}\right)^{\frac{1}{2}}$$
 ( $P < P^{\min}$  would make the object disintegrate)  
 $P_{\text{spin}}^{\min} \sim 5 \times 10^{-4}$  for a neutron star.  
 $P_{\text{spin}}^{\min} \sim 1.5$  hours for Earth.  
 $P_{\text{spin}} = 1.396 \times 10^{-3}$  s for PSR J1748-2446ad; Hessels J. W. T. et al., Science, 311, 1901 (2006)

# **Dimensions :**

•  $M \sim 1-3~{
m M}_{\odot}~~({
m M}_{\odot} \sim 2 imes 10^{33}~{
m gm})$ 

•  $R \sim 10-15~{
m Km}$ 

# **Compact Structure : Consequences**

• Strong Magnetic Field : 
$$P^{
m G}_{
m central}~(rac{Gm^2}{R^4})\gtrsim~P^{
m EM}~(rac{B^2}{8\pi})$$

 $B_{\rm max} \sim 10^{18}$  G for a neutron star.

 $B_{\rm s}\sim$  2.06  $\times$  10<sup>15</sup> G for PSR J1808-2024; Mereghetti, S. et al., ApJ, 628, 938 (2005)

# **Magnetic Field of Astrophysical Objects**

	$\begin{array}{c} \text{mass} \\ \mathrm{M}_{\odot} \end{array}$	radius cm	B <sup>surface</sup> G	B <sup>central</sup> G
Earth Jupiter Brown Dwarf Sun White Dwarf Neutron Star	$10^{-6} \\ 10^{-3} \\ 0.01 - 0.8 \\ 1.0 \\ \simeq 1.4 \\ 1.0 - 3.0$	$\begin{array}{c} 6\times 10^8 \\ 7\times 10^9 \\ 10^{10} \\ 10^{11} \\ 10^9 \\ 10^6 \end{array}$	$ \begin{array}{l} \lesssim 1 \\ \sim 10 \\ 1 - 10^3 \\ \sim \text{few} \\ 10^3 - 10^9 \\ 10^8 - 10^{15} \end{array} $	$10^{7} \\ 10^{7} \\ 10^{7} - 10^{8} \\ 10^{8} \\ 10^{12} \\ 10^{18} \\ 10^{18} \\$

# **Dimensions :**

- $M \sim 1-3~{
  m M}_{\odot}~~({
  m M}_{\odot}\sim 2 imes 10^{33}~{
  m gm})$
- $R \sim 10 15 \text{ Km}$ •  $ho_{\rm av.} \sim 10^{14} - 10^{15} \text{ g cm}^{-3}$  ( $ho_{\rm nuc} \sim 2.3 \times 10^{14} \text{ g cm}^{-3}$ )

# **High Density : Consequences**

- Degenerate Material :  $T_F (E_F = k_B T_F) >> T_{NS}$ electrons - degenerate, relativistic protons - degenerate, non-relativistic neutrons - degenerate, non-relativistic
- A high density, zero temperature system.

# **The Radio Pulsar**

# **Radio Pulsar**



# **Radio Pulsar**





# **Radio Profile**



- wide variation in pulse shapes
- different shape at different energies

Image Credit : Jodrell Bank Observatory

# **High-Energy Profile**



Image Credit : Jodrell Bank Observatory

#### Magnetosphere



Image Credit : NASA

### Magnetosphere



Image Credit : NASA

Magnetosphere - field dominated :

 $F_{\rm G}/F_{\rm EM} \simeq \frac{GMm_e}{r^2} / \frac{e\Omega rB}{c} \simeq 10^{-12}$ for  $B \sim 10^{12}$  G,  $P_s \sim 1$  s  $F_{\rm G}$  - gravitational force on an electron

 $\textit{F}_{\rm EM}$  - electromagnetic force on an electron

**Magnetosphere - force-free :**   $\mathbf{E} + \frac{1}{c}(\Omega \times \mathbf{v}) \times \mathbf{B} = \mathbf{0} \Rightarrow \delta n = \frac{\Omega \cdot \mathbf{B}}{2\pi ec}$   $\mathbf{E}$  - induced electric field  $\delta n$  - net charge density

# Brightness Temperature (T<sub>B</sub>) of an Emitting Region

- $I_{\nu} = B_{\nu}(T_B) = rac{2h\nu^3}{c^2}rac{1}{e^{rac{h\nu}{K_{\mathrm{B}}T_B}}-1}$ 
  - $\boldsymbol{\nu}$  frequency of radiation
  - $I_{\nu}$  specific intensity
  - $B_{\nu}$  Planck function (blackbody radiation)

# Rayleigh-Jeans Law

- $I_{\nu} = rac{2
  u^2}{c^2} k_{
  m B} T_B$  for  $h
  u << k_{
  m B} T_B$ 
  - T<sub>B</sub> blackbody temperature
  - k<sub>B</sub> Boltzmann constant

# **Pulsar Radiation :**

- $I_{\nu} \sim 10^4 10^7 \ erg.s^{-1}.cm^{-2}.Hz^{-1}.sr^{-1}$  $T_b \sim 10^{23} - 10^{26} \ K$
- absurdly high blackbody temperature
- unfeasible particle energies
- radiation in higher frequency (than radio)

# pulsar emission $\neq$ blackbody radiation

## **Dipolar Model**

$$\mathbf{m} = \frac{1}{2} B_{\rho} R^{3} \left( \cos \alpha \, \mathbf{e}_{||} + \sin \alpha \, \cos \Omega t \, \mathbf{e}_{\perp} + \sin \alpha \, \sin \Omega t \, \mathbf{e}'_{\perp} \right)$$
$$\Rightarrow m = \frac{1}{2} B_{\rho} R^{3}$$





# Rotating Dipole $\rightarrow$ Time Variability $\rightarrow$ Radiation

**Radiative Energy**:  $\vec{E}_{rad} = -\frac{2}{3c^3} |\ddot{\mathbf{m}}|^2 = -\frac{1}{6c^3} B_p^2 R^6 \Omega^4 \sin^2 \alpha$  **Rotational Energy**:  $E_{rot} = \frac{1}{2} I \Omega^2 \Rightarrow \vec{E}_{rot} = I \Omega \dot{\Omega}$  **Dipolar Field**:  $E_{rot} = \vec{E}_{rad} \Rightarrow B_p \simeq 3.2 \times 10^{19} (P_s \dot{P}_s)^{1/2}$  **Radiation slow-down**:  $\vec{E}_{rot} < 0 \Rightarrow \dot{\Omega} < 0$ **Characteristic Age**:  $\tau_{ch} = \frac{P_s}{2\dot{P}}$  for  $P_s^\circ << P_s (P_s^\circ - \text{initial spin-period})$ 

# **Radio Pulsar : The Model**



- fast rotation + strong magnetic field  $\Rightarrow$  strong electric field acceleration of charged particles  $\rightarrow$  radiation energetic radiation  $\rightarrow$  pair production
- synchrotron radiation, Compton scattering, (radio radiation mainly from) curvature radiation
  - $P_{\rm spin} \sim 10^{-3} 10^{1.5} \, {\rm s}$
  - $B_{\rm surface} \sim 10^8 10^{15} \, {\rm G}$
  - $\vec{E}_{\rm rot} \propto I\Omega\dot{\Omega} \propto \Omega^4 B^2$  dipole model

# Gravitational Radiation at the cost of Rotational Energy

 $\dot{E_{\rm GW}} < 0 \ 
ightarrow \dot{\Omega} < 0$ 

# Rotating Mass Quadrupole Moment $\rightarrow$ Gravitational Radiation

 $\dot{E_{\mathrm{GW}}} = I\Omega\,\dot{\Omega} = -rac{32}{5}rac{G}{c^5}I^2\,\epsilon\Omega^6$ 

 $\epsilon$  - ellipticity *G* - gravitational constant

Characteristic Age :  $\tau_{ch}$  (gravitational)

Typically :  $\tau_{ch}(EM) << \tau_{ch}(GW)$ 

Actual slow-down is a combination of EM and GW radiation.

# **Power Law Deceleration**

$$\dot{\Omega}=-(\mathit{constant})\,\Omega^n\,
ightarrow n=-rac{\Omega\ddot{\Omega}}{\dot{\Omega}^2}$$

n - braking index

n = 3 : magnetic dipole radiation

n < 3 : magnetic dipole radiation + alignment..

- n < 3 : higher magnetic multipoles
- n = 5 : gravitational radiation
- n = 3.43 : Crab Pulsar (combination effects)

# **Timing & Null**

# **Precision Timing**



 $\dot{P} \sim 5 imes 10^{-22} - 5 imes 10^{-10}$  s/s

The fractional stability of millisecond pulsars compared to an atomic clock. B1855+09 and B1937+21 are comparable (just slightly worse) to the atomic clock over timescales of years. J0437-4715 is inherently stable.

# **Gravitational Physics : Pulsar Timing Array**



Figure : http://gwplotter.com/

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#### Introduction Timing & Null

#### **Extrasolar Planet Detection**



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# **Time of Arrival**



Figure Credit : Lorimer D.R., Living Reviews in Relativity, 11, 8 (2008)



# TOA : time of arrival

refers to a fiducial point on profile

delay with respect to a template profile

$$\mathcal{P}(t) = \mathbf{a} + \mathbf{b}\mathcal{T}(t-\tau) + \mathcal{N}(t)$$

- •P(t) observed profile
- •T(t) template profile
- •N(t) noise
- ullet au time shift

#### **Isolated Pulsars**

# **Time Delay**

$$t_{\rm SSB} = t_{
m topo} + t_{
m corr} - \Delta/f^2 + \Delta_{R_{\odot}} + \Delta_{S_{\odot}} + \Delta_{E_{\odot}}$$

- t<sub>SSB</sub> solar system barycentric delay
- $t_{topo}$  topocentric delay
- *t*<sub>corr</sub> clock corrections
- $\Delta/f^2$  correction for dispersion measure
- $\Delta_{R_{\odot}}$  Romer delay (light-travel time from telescope to SSB)
- $\Delta_{S_{\odot}}$  Shapiro delay (correction for spacetime curvature)
- $\Delta_{E_{\infty}}$  Einstein delay (gravitational redshift + time dilation)

# **Nulling Pulsars**



# Radio Pulsar

# Nulling Pulsar

**Extreme Nulling** 

RRAT

# **Nulling Behaviour**



Figure credit : Wang N., Manchester R. N., Johnston S., MNRAS, 377, 1383 (2007)

# **Drifting Subpulses**



Figure credit : Deshpande, A. A., Rankin, J. M., ApJ, 524, 1008 (1999)

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# **Mode Changing**



PSR B0943+10 - radio & X-ray brightness switched Hermsen W. et al., Science, 339, 436 (2013)

Image credit : ESA/ATG medialab; ESA/XMM-Newton; ASTRON/LOFAR

# **Nulling Behaviour**



Figure credit : Wang N., Manchester R. N., Johnston S., MNRAS, 377, 1383 (2007)

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- null abrupt cessation of pulsed emission
- association with drifting of subpulses
- association with mode changes
- association with switching emission frequencies
- association with change in  $\dot{P}_s$

### **Population Characteristics**

- $\bullet$  ~ 200 nulling pulsars
- $0.5s \lesssim P_s \lesssim 10.0s$
- $\bullet~10^{11}~G \lesssim \textit{B}_{s} \lesssim~10^{13}~G$
- $10^6 \ \mathrm{Yr} \lesssim \, au_{\mathrm{ch}} \lesssim \, 10^8 \ \mathrm{Yr}$
- $\bullet~10~pc.cm^{-3} \lesssim~\textit{DM} \lesssim~10^3~pc.cm^{-3}$

# **Nulling Pulsars II**

# **Characterising Parameters**

- nulling fraction (NF)  $\leq$  95%
- null length (NL) [not much data]
- neither NL or NF is an unique marker

# NP Classes (NL)

- classical nuller a few pulses
- intermediate nuller up-to a few hours
- intermittent pulsar even years
- RRAT characterised by single pulse emission

### Radio Pulsar : Age

- P- current pulsar period
- P<sub>0</sub> initial pulsar period
- P- current period derivative
- B- current dipolar magnetic field
- $\tau_{p}$  current pulsar age

$$B = a(P\dot{P})^{1/2} \Rightarrow$$
  

$$\tau_{p} = \frac{1}{2}a^{2}(P^{2} - P_{0}^{2})B^{-2}$$
  

$$\simeq \frac{1}{2}a^{2}P^{2}B^{-2} \simeq (P_{0} << P)$$

 $\tau_{c} = \left(\frac{P}{2\dot{P}}\right)$ , constant *B* justified over radio pulsar lifetime (~ 10<sup>6</sup> year).

(1)

#### **Radio Pulsar : Life Expectancy**

 $\log B = a_1(\log P + \log \dot{P}), \text{ dipolar field}$  $\tau_p = a_3 P^2 B^{-2}, \text{ current age}$ 

$$\begin{array}{rcl} \log B &=& a_2 \log P + b_2 \log \dot{P}, & \text{death-line} \\ \tau_t &=& a_4 P_D^2 B^{-2}, & \text{age at death} \\ P_D &=& f(B), & \text{period at death} \end{array}$$

$$\epsilon_{\text{proximity}} = \frac{\tau_t - \tau_{\rho}}{\tau_t}$$
, death-line proximity parameter

# Nulling not correlated with $\epsilon_{\text{proximity}}$ .

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#### Introduction Timing & Null

# **Nulling Pulsars : Death-line**



# **The Resources**

# **Resource I : Suggested Reading**

- Can Stars Find Peace? G. Srinivasan
- *Pulsars* R. N. Manchester and J. H. Taylor
- *Pulsar Astronomy* A. Lyne and F. Graham-Smith
- Handbook of Pulsar Astronomy D. R. Lorimer and M. Kramer
- Stellar Remnants : Saas-Fee Advanced Course 25 S. D. Kawaler, I. Novikov and G. Srinivasan
- Black Holes, White Dwarfs and Neutron Stars S. L. Shapiro and S. A. Teukolsky

### **Resource II : Database**

• *Pulsars(ATNF)* : http://www.atnf.csiro.au/research/pulsar/psrcat/

• Globular Cluster Pulsars (Paulo Freire) : http://www.naic.edu/~pfreire/GCpsr.html

- Galactic Millisecond Pulsars :
   http://astro.phys.wvu.edu/GalacticMSPs/
- AXPs, SGRs, Magnetars (McGill) : http://www.physics.mcgill.ca/ pulsar/magnetar/main.html
- X-Ray Pulsars (Remeis-Sternwarte) :

https://www.sternwarte.uni-erlangen.de/wiki/index.php/List-of-accreting-X-ray-pulsars

• *Glitching Pulsars (Jodrell Bank) :* http://www.jodrellbank.manchester.ac.uk/research/research-groups/pulsars-and-time-domainastrophysics/glitches-pulsars/

Gamma-Ray Pulsars (LAT):
 https://confluence.slac.stanford.edu/display/GLAMCOG/Public+List+of+LAT-Detected+Gamma-Ray+Pulsars

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